

**REPORT DOCUMENTATION PAGE**Form Approved  
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Washington Headquarters Service, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188) Washington, DC 20503.

**PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.****1. REPORT DATE (DD-MM-YYYY)****2. REPORT TYPE**

Final

**3. DATES COVERED (From - To)**

05/2003 - 10/2006

**4. TITLE AND SUBTITLE**

Asymptotic Analysis of Melt Growth for Antimonide-Based Compound Semiconductor Crystals in Magnetic and Electric Fields

**5a. CONTRACT NUMBER****5b. GRANT NUMBER**

FA9550-04-1-0249

**5c. PROGRAM ELEMENT NUMBER****5d. PROJECT NUMBER****5e. TASK NUMBER****5f. WORK UNIT NUMBER****6. AUTHOR(S)**

Nancy Ma

**7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)**North Carolina State University  
Campus Box 7910, 2601 Stinson Drive  
Raleigh, NC 27695-7910**8. PERFORMING ORGANIZATION  
REPORT NUMBER****9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)**Dr. Arje Nachman  
Air Force Office of Scientific Research  
875 North Randolph St., Rm 3112  
Arlington, VA 22203**10. SPONSOR/MONITOR'S ACRONYM(S)****20071024063****12. DISTRIBUTION AVAILABILITY STATEMENT**

DISTRIBUTION A. Approved for public release; distribution unlimited.

AFRL-SR-AR-TR-07-0426

**13. SUPPLEMENTARY NOTES****14. ABSTRACT**

Single crystals of doped and alloyed antimonide-based semiconductors are needed for Air Force Applications because they serve as transparent, lattice-matched epitaxial growth templates for detectors. High-performance devices rely on good compositional homogeneity in the bulk substrate which is cut from wafers sliced from the crystal. Several important processes are being developed at AFRL in Hanscom AFB, which are the vertical gradient freezing process using submerged heater growth, the vertical Bridgman process using submerged heater growth, and the magnetic liquid-encapsulated Czochralski process. Because molten semiconductors are excellent electrical conductors, these processes apply magnetic and electric fields to control the melt motion and thus the convective transport of species during growth in order to optimize the properties of the crystal. Asymptotic and numerical modelling of these processes have provided predictions of the transport in the melt and of the compositional distribution in the crystal.

**15. SUBJECT TERMS**

Semiconductor crystal growth, asymptotics

**16. SECURITY CLASSIFICATION OF:****17. LIMITATION OF  
ABSTRACT**  
U**18. NUMBER  
OF PAGES****19a. NAME OF RESPONSIBLE PERSON**  
Nancy Ma**a. REPORT**  
U**b. ABSTRACT**  
U**c. THIS PAGE**  
U**19b. TELEPHONE NUMBER (Include area code)**  
919-515-5231



## Final Report for AFOSR Grant FA9550-04-1-0249

### TECHNICAL SUMMARY

Three important processes which are used to grow single crystals of semiconductors are being developed at AFRL in Hanscom AFB which are the vertical gradient freezing process using submerged heater growth, the vertical Bridgman process using submerged heater growth, and the magnetic liquid-encapsulated Czochralski process. These processes as well as the Bridgman-Stockbarger process have been investigated. During the growth of any semiconductor, a major objective is to minimize segregation of dopant or alloy components in the crystal. Because molten semiconductors are excellent electrical conductors, magnetic fields or electric fields or a combination of both can be used to control the melt motion and thus the convective species transport during growth in order to promote compositional homogeneity. Asymptotic and numerical models using Chebyshev spectral collocation methods are developed. Key results are summarized here.

The traditional Bridgman-Stockbarger process in steady magnetic fields produces crystals with severe segregation. Therefore other means are needed to optimize the crystal growth process in order to produce crystals with minimal segregation. The vertical gradient freezing process using a submerged heater in a combination of steady magnetic and electric fields produced crystals with axial uniformity and with little radial segregation. The vertical Bridgman process in rotating magnetic fields also produced crystal with axial uniformity and with little radial segregation, but a crystal growth in combination of magnetic and electric fields with the equivalent parameters produced a crystal with less segregation. Investigations of magnetic liquid-encapsulated Czochralski crystal growth in rotating magnetic fields are in progress and preliminary results indicate that this is a promising means to minimize radial segregation.

### PEOPLE INVOLVED

Dr. P. Becla, Solid State Scientific, Hollis, NH

Dr. D. F. Bliss, Sensors Directorate, U.S. Air Force Research Laboratory, Hanscom AFB, MA

Dr. G. G. Bryant, Sensors Directorate, U.S. Air Force Research Laboratory, Hanscom AFB, MA

Dr. G. W. Iseler, Iseler Associates, Chelmsford, MA

### JOURNAL ARTICLES

1. Xianghong Wang, Nancy Ma, David F. Bliss, Gerald W. Iseler and Piotr Becla, "Combining static and rotating magnetic fields during modified vertical Bridgman crystal growth," *AIAA Journal of Thermophysics and Heat Transfer*, submitted.
2. Mei Yang, Nancy Ma, David F. Bliss and George G. Bryant, "Melt motion during liquid-encapsulated Czochralski crystal growth in steady and transverse rotating magnetic fields," *International Journal of Heat and Fluid Flow*, accepted.
3. Xianghong Wang and Nancy Ma, "Semiconductor crystal growth by the vertical Bridgman process with rotating magnetic fields," *ASME Journal of Heat Transfer*, accepted.
4. Xianghong Wang, Nancy Ma, David F. Bliss and Gerald W. Iseler, "Solute segregation during modified vertical gradient freezing of alloyed compound semiconductor crystals with magnetic and electric fields," *International Journal of Heat and Mass Transfer*, vol. 49, no. 19/20, pp. 3429-3438, September 2006.
5. Xianghong Wang, Nancy Ma, David F. Bliss, Gerald W. Iseler and Piotr Becla, "Parametric study of modified vertical Bridgman growth in a rotating magnetic field," *AIAA Journal of*



*Thermophysics and Heat Transfer*, vol. 20, no. 3, pp. 384-388, July-September 2006.

6. Nancy Ma and John S. Walker, "Strong-field electromagnetic stirring in the vertical gradient freeze process with a submerged heater," *Journal of Crystal Growth*, vol. 291, no. 1, pp. 249-257, May 2006.
7. Xianghong Wang and Nancy Ma, "Bridgman-Stockbarger growth of binary alloyed semiconductor crystals with steady magnetic fields," *AIAA Journal of Thermophysics and Heat Transfer*, vol. 20, no. 2, pp. 313-319, April-June 2006.
8. Xianghong Wang, Nancy Ma, David F. Bliss, Gerald W. Iseler and Piotr Becla, "Comparing modified vertical gradient freezing with rotating magnetic fields or with steady magnetic and electric fields," *Journal of Crystal Growth*, vol. 287, no. 2, pp. 270-274, January 2006.
9. Nancy Ma and John S. Walker, "Electromagnetic stirring in crystal growth processes," *Fluid Dynamics & Materials Processing*, vol. 2, no. 2, pp. 119-125, 2006.
10. Mei Yang and Nancy Ma, "A computational study of natural convection in a liquid-encapsulated molten semiconductor with a horizontal magnetic field," *International Journal of Heat and Fluid Flow*, vol. 26, no. 5, pp. 810-816, October 2005.
11. Amy M. Holmes, Xianghong Wang, Nancy Ma, David F. Bliss and Gerald W. Iseler, "Vertical gradient freezing using submerged heater growth with rotation and with weak magnetic and electric fields," *International Journal of Heat and Fluid Flow*, vol. 26, no. 5, pp. 792-800, October 2005.
12. Mei Yang and Nancy Ma, "Free convection in a liquid-encapsulated molten semiconductor in a vertical magnetic field," *International Journal of Heat and Mass Transfer*, vol. 48, no. 19/20, pp. 4010-4018, September 2005.
13. Xianghong Wang and Nancy Ma, "Numerical model for Bridgman-Stockbarger crystal growth with a magnetic field," *AIAA Journal of Thermophysics and Heat Transfer*, vol. 19, no. 3, pp. 406-412, July-September 2005.
14. Xianghong Wang, Nancy Ma, David F. Bliss and Gerald W. Iseler, "A numerical investigation of dopant segregation by modified vertical gradient freezing with moderate magnetic and weak electric fields," *International Journal of Engineering Science*, vol. 43, no. 11/12, pp. 908-924, July 2005.
15. Stephen J. LaPointe, Nancy Ma and Donald W. Mueller, Jr., "Growth of binary alloyed semiconductor crystals by the vertical Bridgman-Stockbarger process with a strong magnetic field," *ASME Journal of Fluids Engineering*, vol. 127, no. 3, pp. 523-528, May 2005.
16. Xianghong Wang, Nancy Ma, David F. Bliss and Gerald W. Iseler, "Semiconductor crystal growth by modified vertical gradient freezing with electromagnetic stirring," *AIAA Journal of Thermophysics and Heat Transfer*, vol. 19, no. 1, pp. 95-100, January-March 2005.
17. Mei Yang, Nancy Ma, David F. Bliss and Joseph L. Morton, "Liquid-encapsulated Czochralski growth of doped gallium-antimonide semiconductor crystals using a strong steady magnetic field," *Magnetohydrodynamics*, vol. 41, no. 1, pp. 73-86, 2005.
18. Xianghong Wang and Nancy Ma, "Strong magnetic field asymptotic model for binary alloyed semiconductor crystal growth," *AIAA Journal of Thermophysics and Heat Transfer*, vol. 18, no. 4, pp. 476-480, October-December 2004.
19. Martin V. Farrell and Nancy Ma, "Macrosegregation during alloyed semiconductor crystal growth in strong axial and transverse magnetic fields," *International Journal of Heat and Mass Transfer*, vol. 47, no. 14/16, pp. 3047-3055, July 2004.

#### **CONFERENCE ARTICLE**

1. Xianghong Wang, Nancy Ma, David F. Bliss and Gerald W. Iseler, "Semiconductor crystal growth by modified vertical gradient freezing with electromagnetic stirring," AIAA 43<sup>rd</sup> Aerospace Sciences Meeting and Exhibit, AIAA Paper #2005-0916, Reno, NV, January 2005.

#### **STUDENT THESES & DISSERTATIONS**

1. Mei Yang, "Liquid-encapsulated Czochralski growth of compound semiconductor crystals with steady and rotating magnetic fields," Ph.D. awarded December 2006.
2. Xianghong Wang, "Semiconductor crystal growth by the vertical Bridgman and gradient freezing processes with applied fields," Ph.D. awarded August 2006.
3. Stephen J. LaPointe, "Growth of binary alloyed semiconductor crystals by the vertical Bridgman-Stockbarger process with a strong magnetic field," M.S. awarded December 2004.